



ATP concentration affects enzymatic processes in time and space

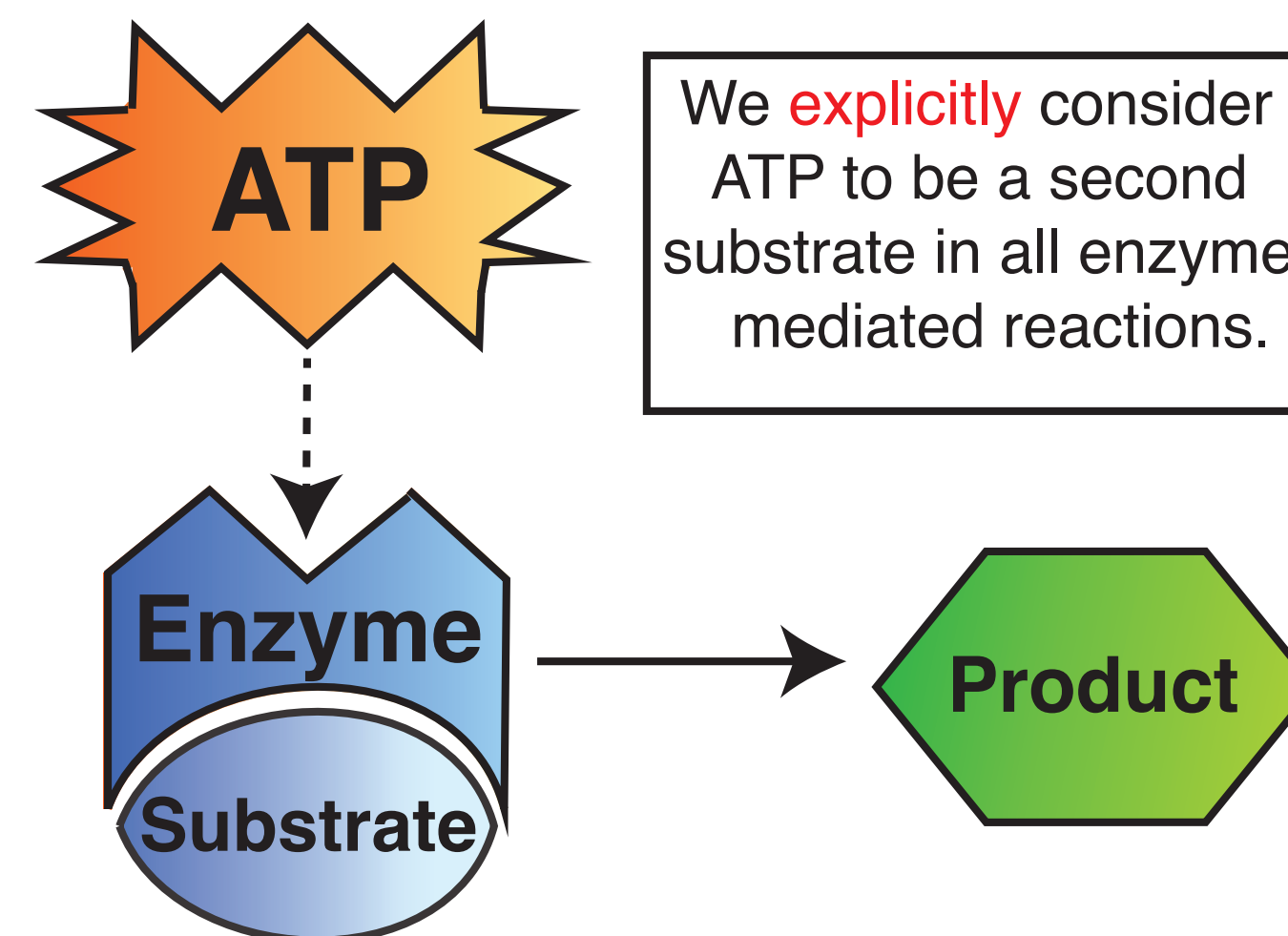
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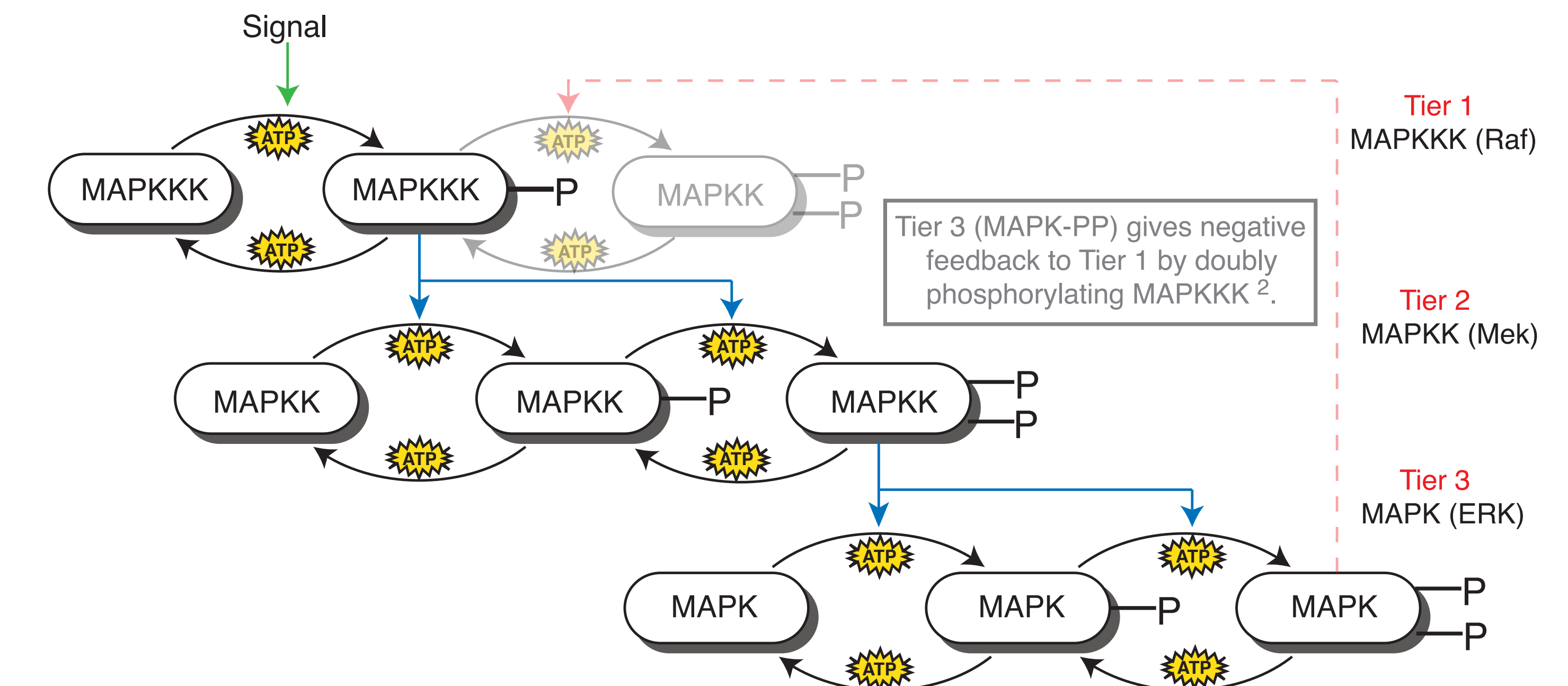
Adenosine 5'-triphosphate (ATP) is the primary "energy currency" of most known living organisms, and thus is a crucial participant in the majority of enzymatic reactions. **In standard enzyme kinetics, ATP is assumed to be continually present in large excess**, therefore allowing enzyme-mediated processes to be modeled as single-substrate reactions and greatly simplifying the associated mathematical analyses. **However, this assumption fails to hold when ATP levels are comparable to substrate levels (e.g., in cellular stress and aging).** Here, we demonstrate the importance of ATP concentration on the dynamics of multi-enzyme reactions by explicit consideration of ATP in enzyme-substrate reactions. **Our results show that the concentration of ATP plays an important role in determining both the time scale and equilibrium concentrations of the substrate and product.**



All reactions are modeled as following **mass action kinetics**.

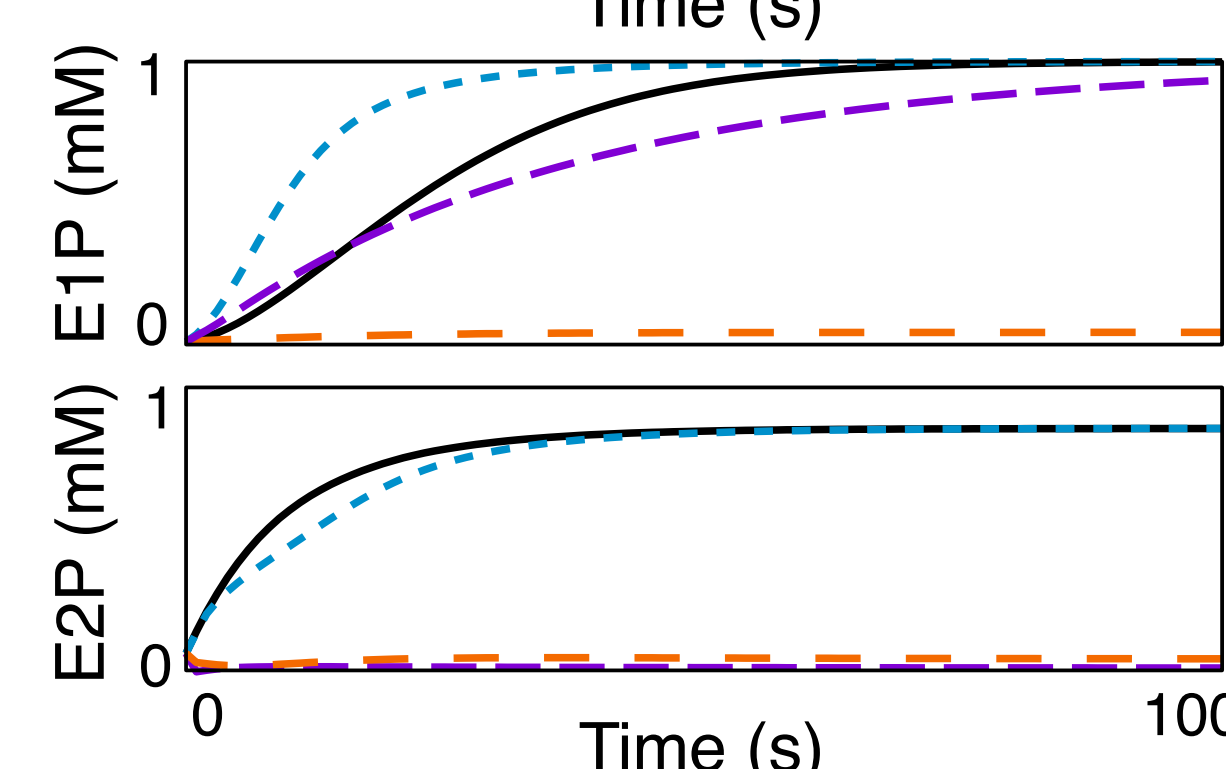
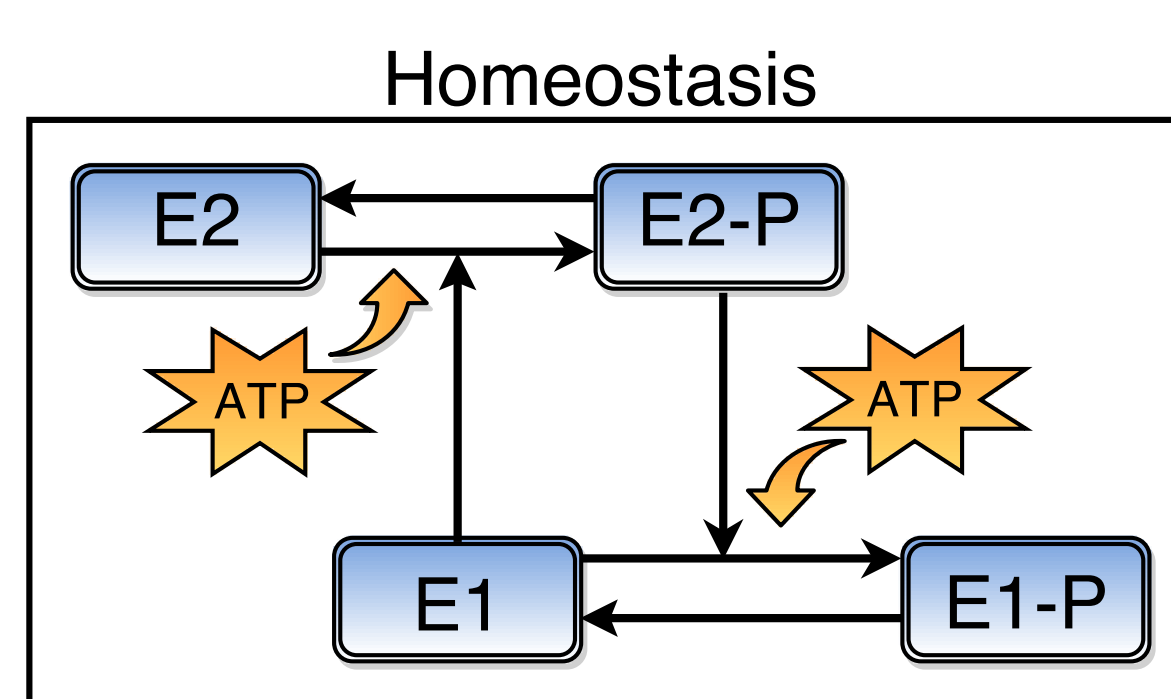
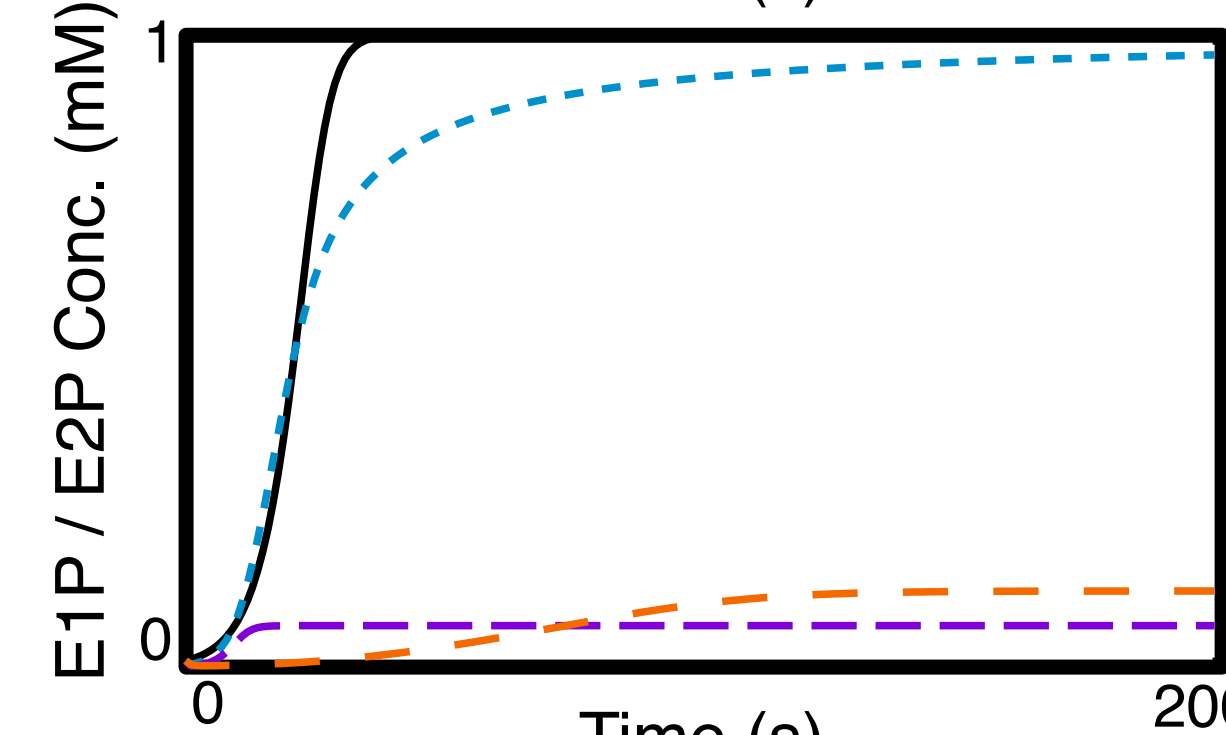
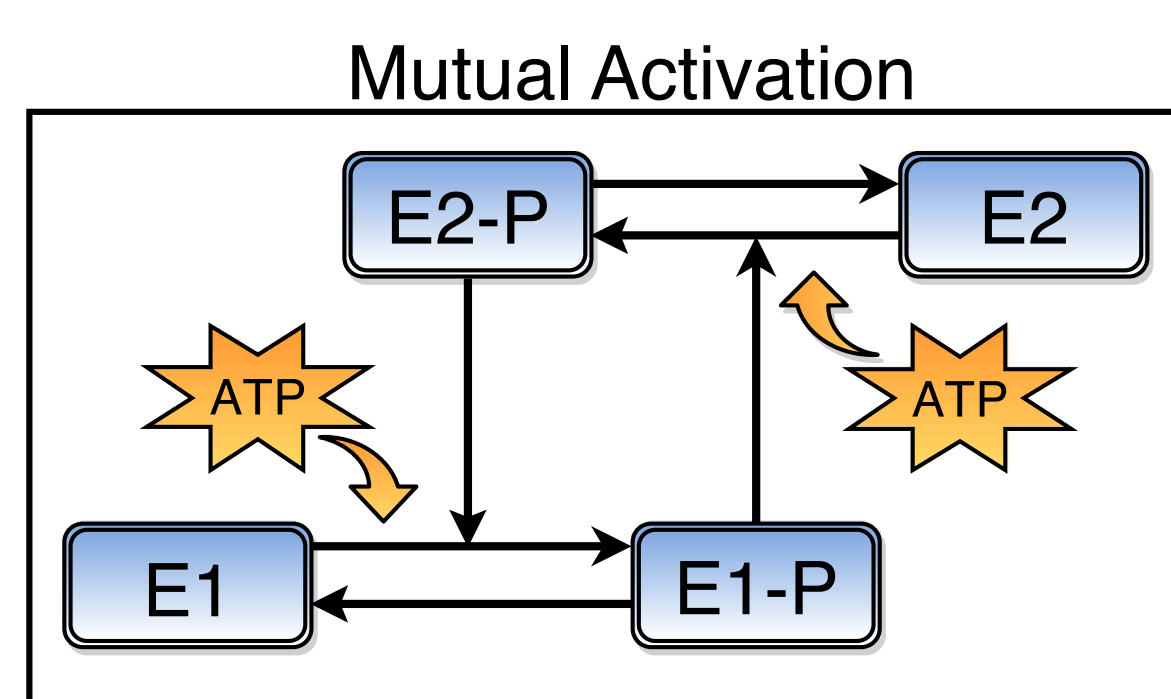
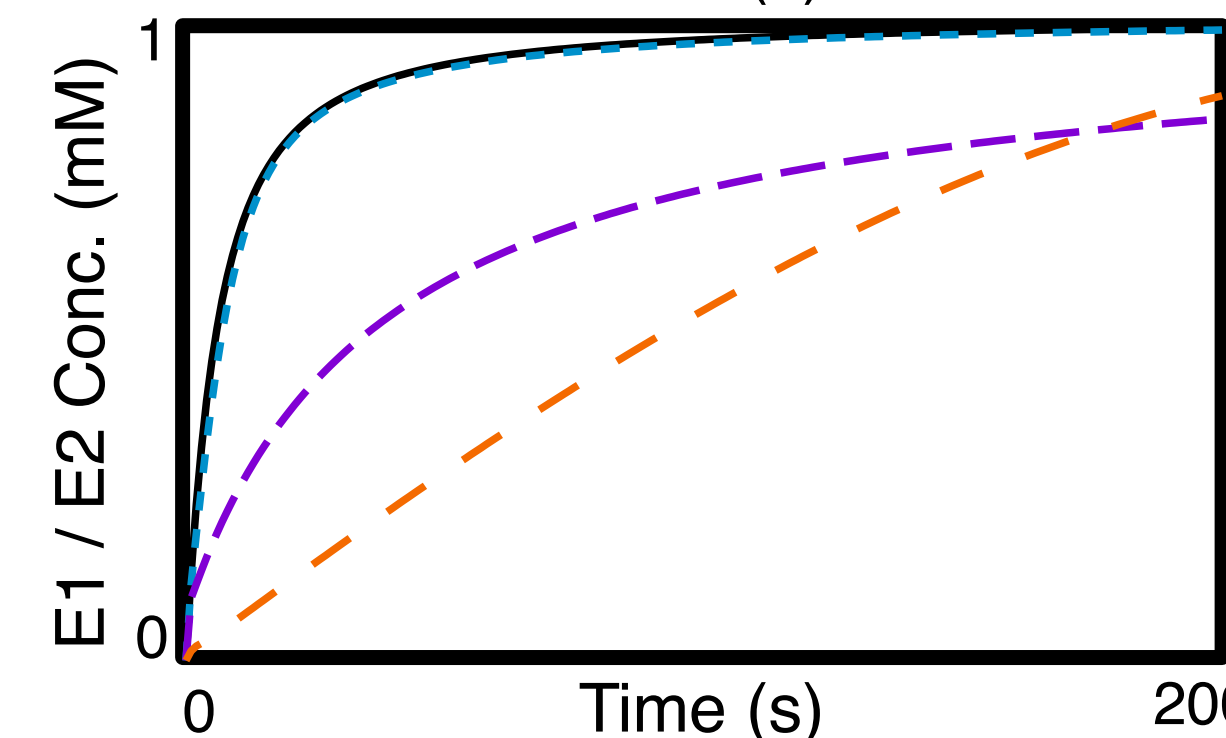
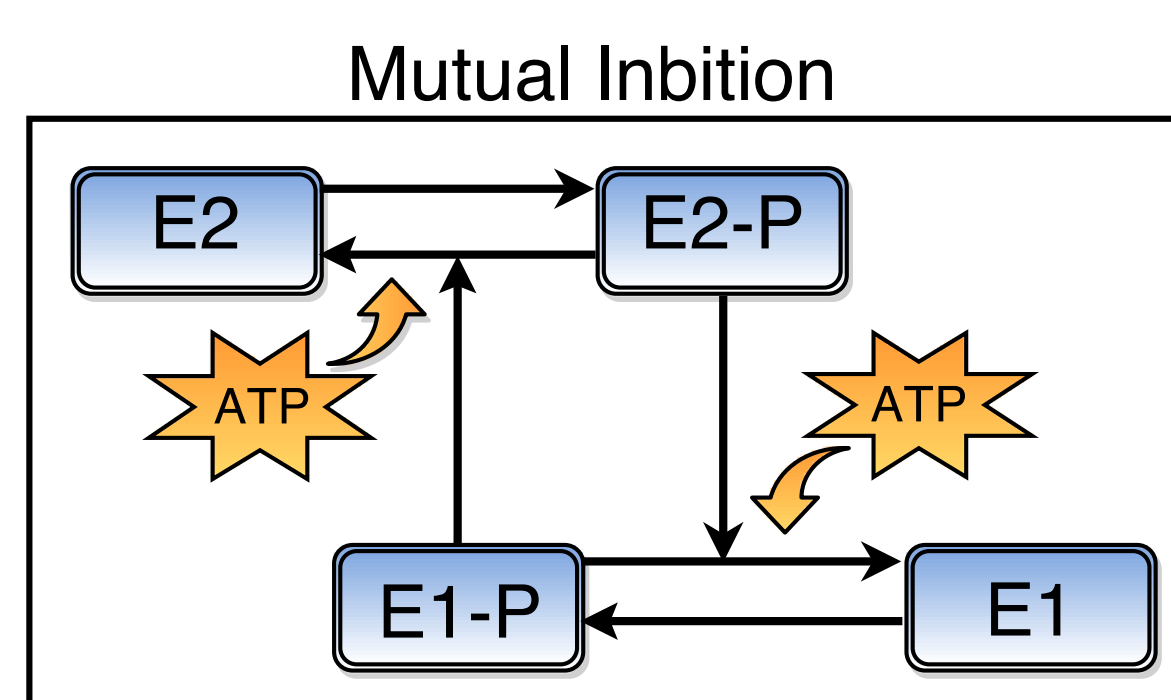
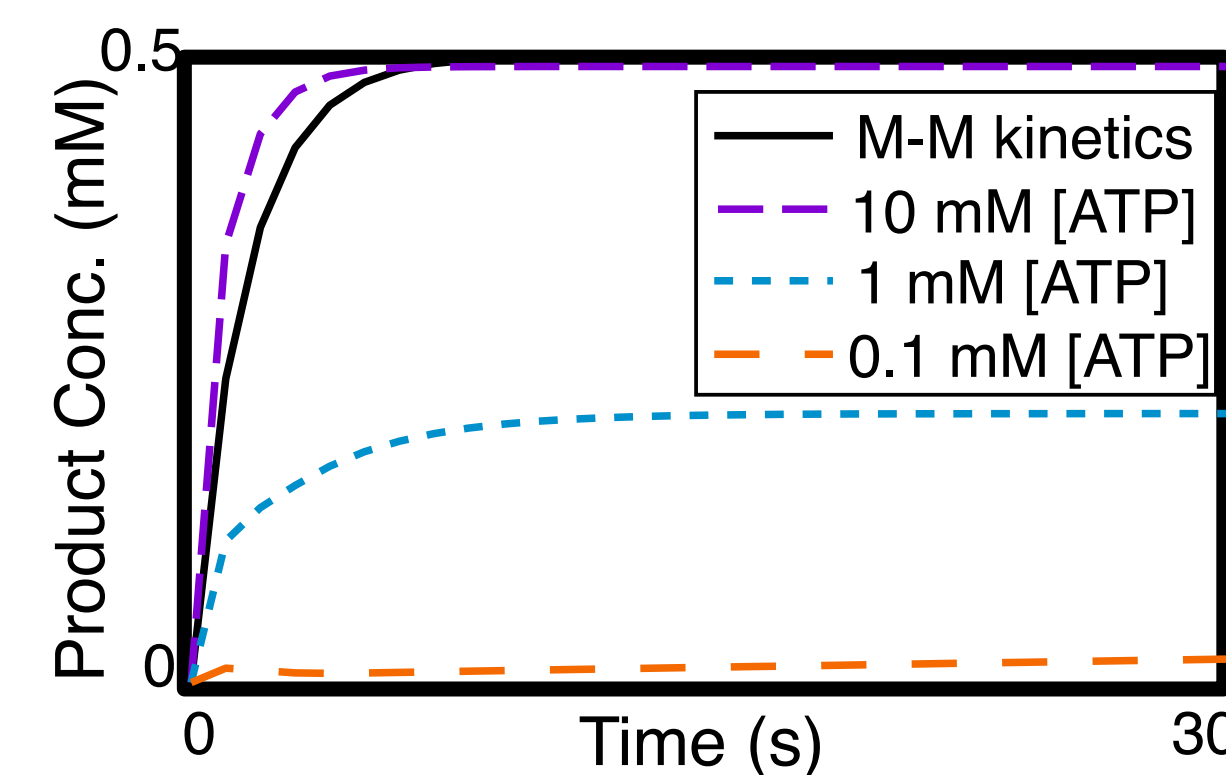
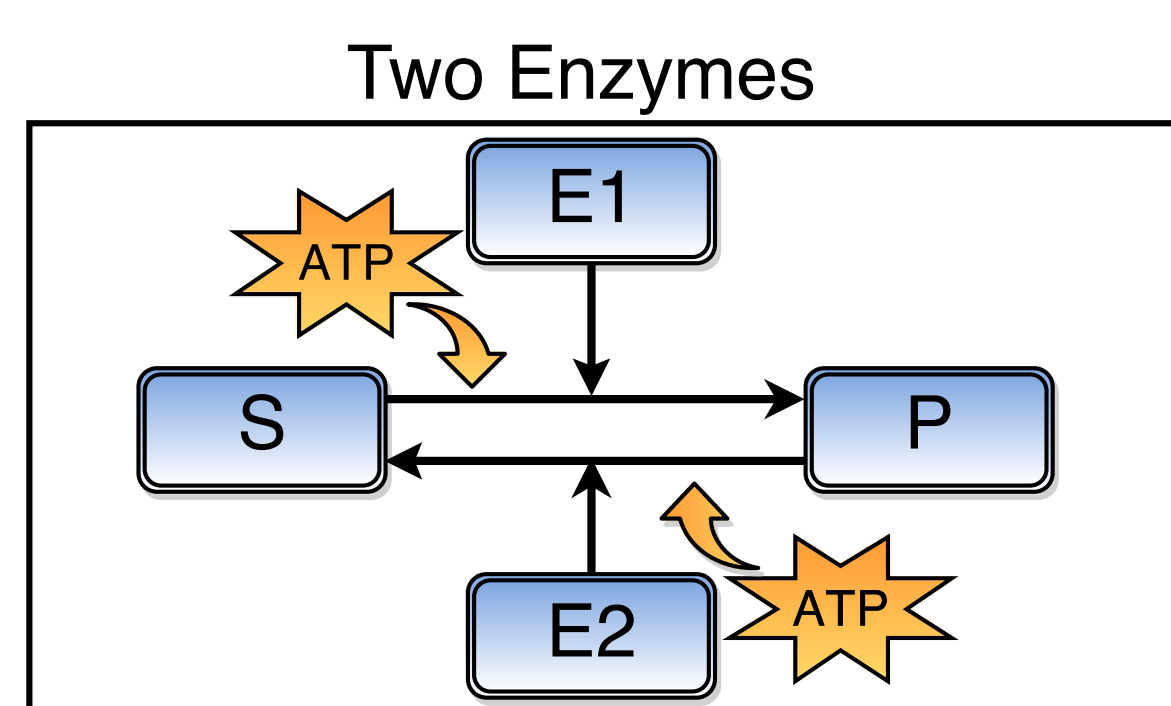
The MAP kinase cascade

The **MAP kinase pathway (or ERK pathway)** is a chain of proteins that is involved in communicating almost all cell surface signals to activate a response in the nucleus.



The three-tiered biochemical signaling pathway¹ is highly conserved and has several characteristic properties, **all of which are significantly affected by ATP concentration**.

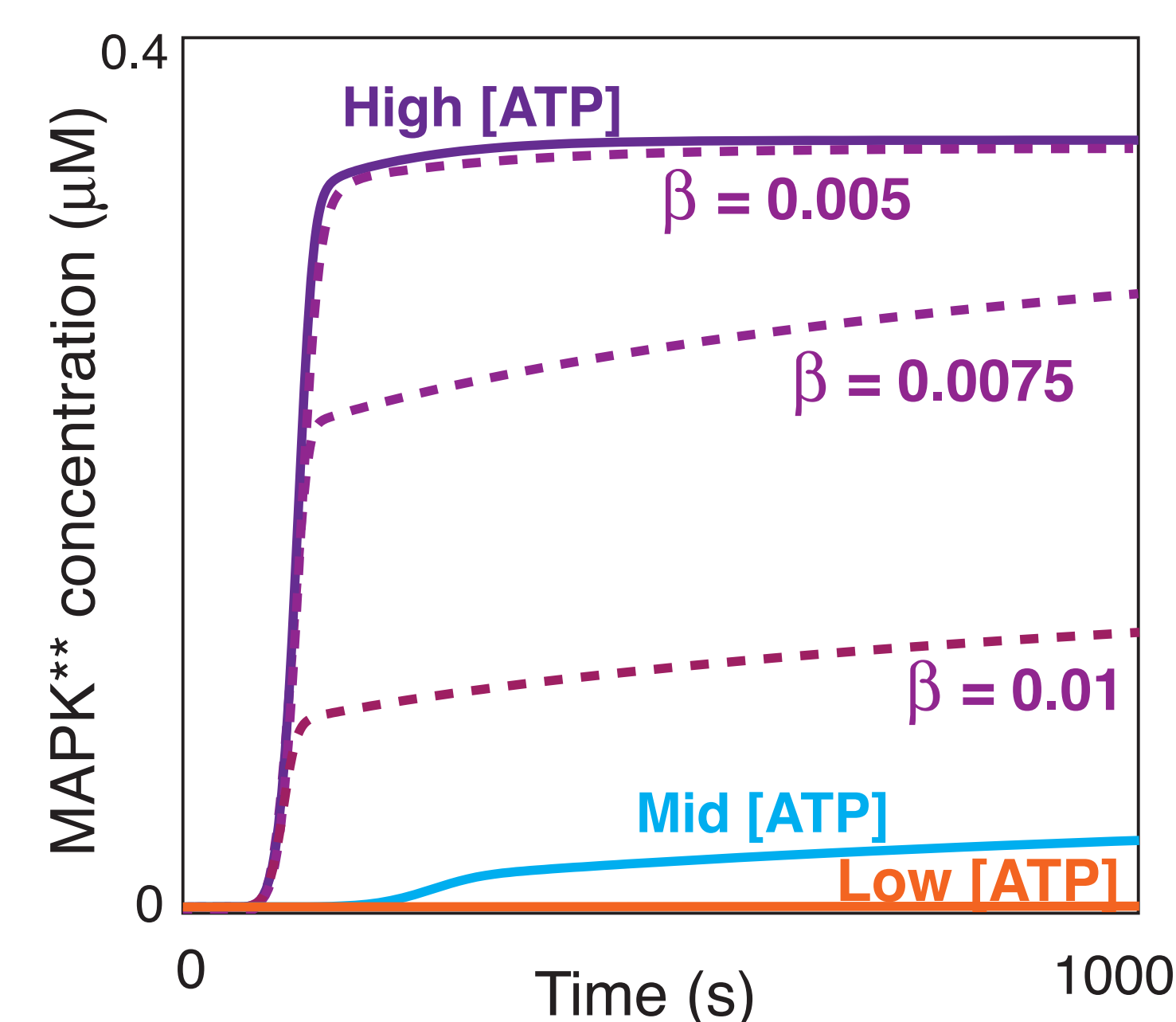
Effects of ATP on simple two-enzyme modules



Characteristics of the MAPK cascade

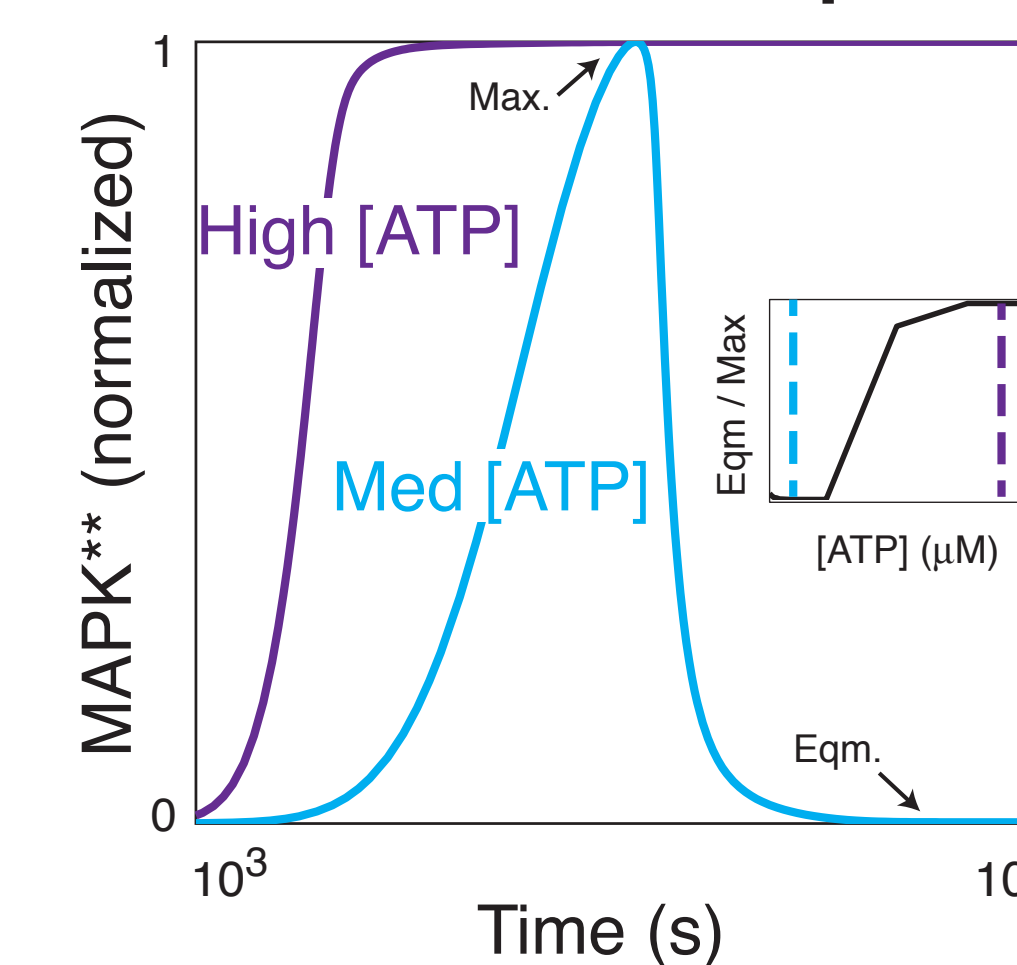
- ▶ **Variable duration** of response
- ▶ **Amplification** of signal
- ▶ **Ultrasensitivity** to stimulus levels

The time course of MAPK activation is **significantly affected** by ATP levels.

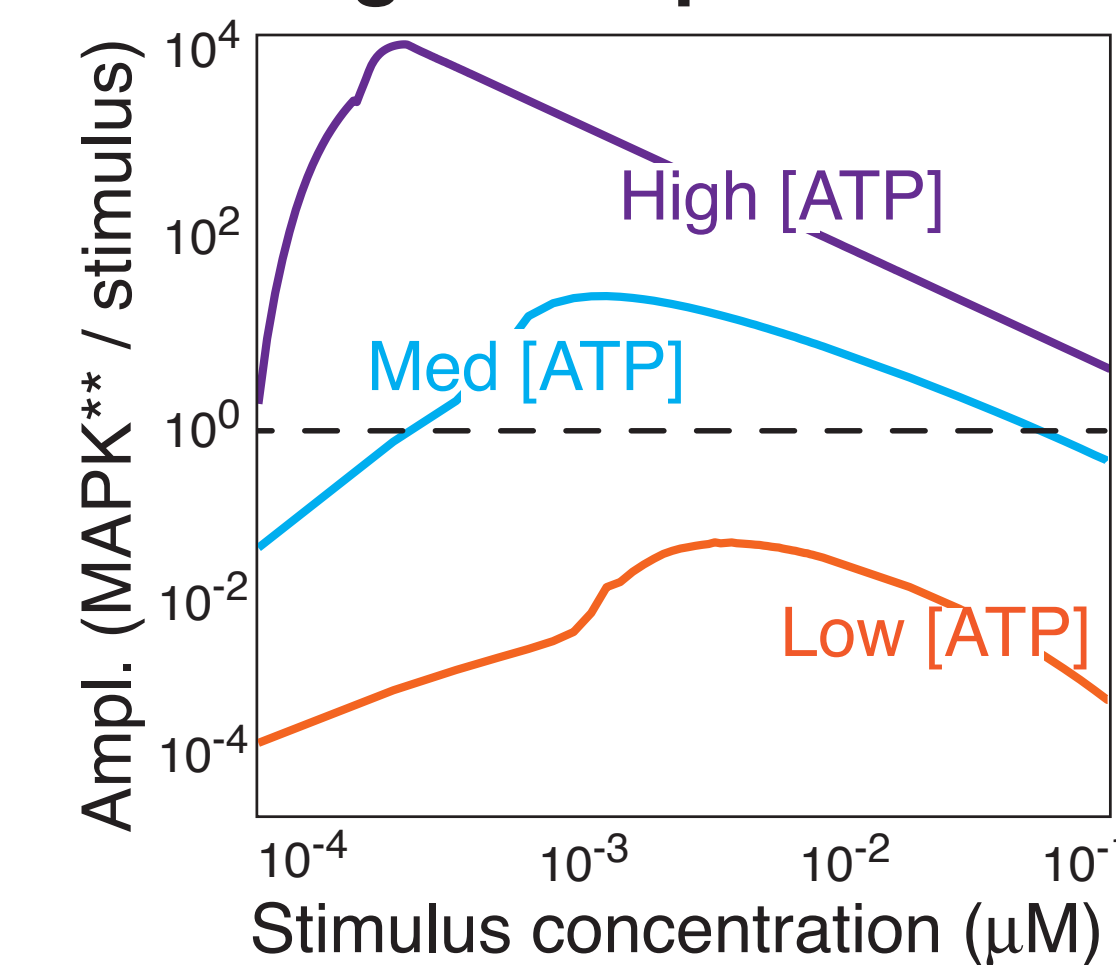


MAPK activation is **robust to sudden cellular stress** only when initial ATP concentrations are saturating (dashed purple lines). This may not be the case in aging cells, **making them more vulnerable to therapeutics**.

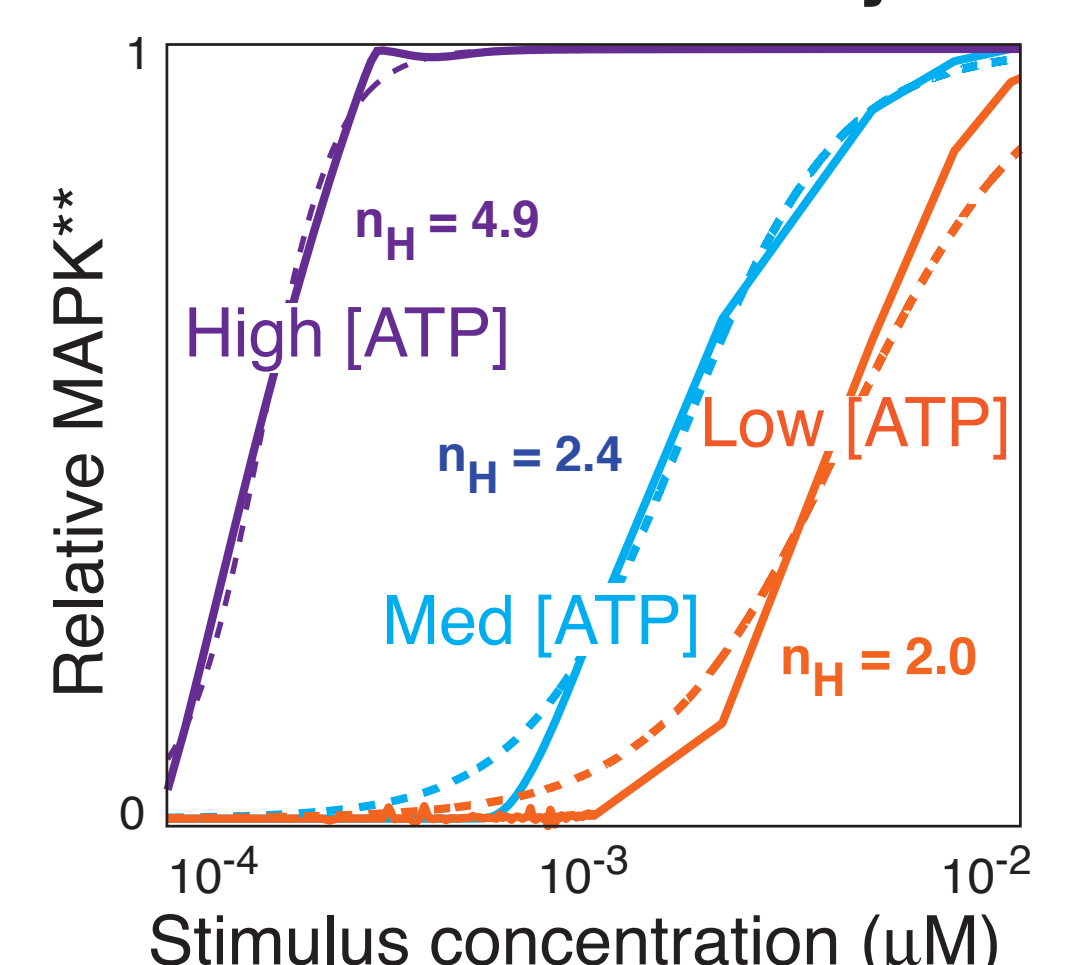
Duration of Response



Signal Amplification

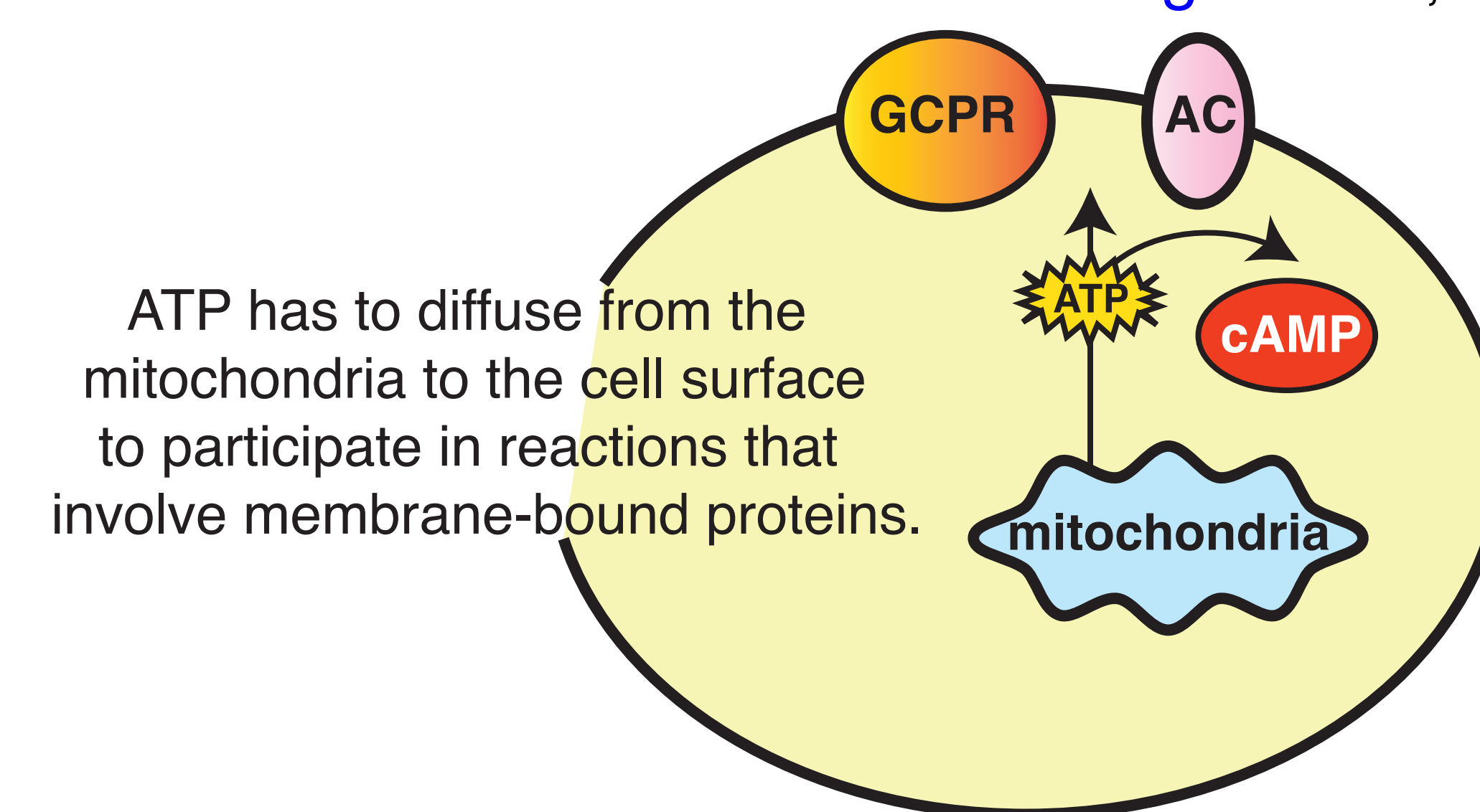


Ultrasensitivity



Future directions

The cellular environment is **not homogeneous**, even with respect to ATP distribution.



ATP participates in many **reactions at the cell membrane** (e.g., generation of cyclic AMP (cAMP), a second messenger in cell-cell signaling).

- ▶ How does the **mitochondrial geometry** affect ATP **spatio-temporal dynamics**?
- ▶ How does the spatial distribution of ATP in the cell **affect production of cAMP**?
- ▶ How does **cAMP compartmentalization** affect the activation of transcription factors in the nucleus?

References

- [1] C.Y. Huang and J.E. Ferrell. *Proc. Nat. Acad. Sci* 93 (1996), 10078–10083.
[2] U.S. Bhalla and R. Iyengar. *Science* 283:5400 (1999), 381–387.

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