

## Section 4.10

**Class Exercise 1.** Verify that  $y_1 = 1$  and  $y_2 = x^2$  are solutions of the differential equation  $yy'' = \frac{1}{2}(y')^2$  but that  $y = c_1y_1 + c_2y_2$  is, in general, not a solution. (#2)

**Exercise 1.** Solve the equation  $y'' = 1 + (y')^2$  by using the substitution  $u = y'$ . (#4)

**Class Exercise 2.** Solve the equation  $e^{-x}y'' = (y')^2$  by using the substitution  $u = y'$ . (#6)

**Exercise 2.** Solve the equation  $(y + 1)y'' = (y')^2$  by using the substitution  $u = y'$ . (#8)

**Class Exercise 3.** Solve the equation  $y^2y'' = y'$  by using the substitution  $u = y'$ . (#10)

**Class Exercise 4.** Solve initial value problem.  
 $y'' + x(y')^2 = 0$ ,  $y(1) = 4$ ,  $y'(1) = 2$ . (#12)

**Exercise 3.** Obtain the first six nonzero terms of a Taylor series solution, centered at 0, of the given initial-value problem. (#18)  
 $y'' + y^2 = 1$ ,  $y(0) = 2$ ,  $y'(0) = 3$

**Class Exercise 5.** Obtain the first six nonzero terms of a Taylor series solution, centered at 0, of the given initial-value problem. (#20)  
 $y'' = e^y$ ,  $y(0) = 0$ ,  $y'(0) = -1$

Homework: 1, 5, 9, 11, 15, 17