



$$\begin{aligned}
 BE &= 2r \\
 DG &= r \\
 AH &= 1/2 \\
 FH &= \sqrt{3}/4 - r/2 \\
 DF &= \sqrt{3}/4 - 3r/2
 \end{aligned}$$

$$\begin{aligned}
 FH/AH &= FG/DG \\
 FG &= \sqrt{DF^2 - DG^2}
 \end{aligned}$$

$\Rightarrow$

$$r = [\sqrt{3} - \sqrt{2}]/2$$