

Transport Research Arena– Europe 2012

# Congestion Control in Urban Networks via Feedback Gating

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## Abstract

Traffic signal control for urban road networks has been an area of intensive research efforts for several decades, and various algorithms and tools have been developed and implemented to increase the network traffic flow efficiency. Despite the continuous advances in the field of traffic control under saturated conditions, novel and promising developments of simple concepts in this area remains a significant objective, because some proposed approaches that are based on various meta-heuristic optimization algorithms can hardly be used in a real-time environment. To address this problem, the recently developed notion of network fundamental diagram for urban networks is exploited to improve mobility in saturated traffic conditions via application of gating measures, based on an appropriate feedback control structure. As a case study, the proposed methodology is applied to the urban network of Chania, Greece, using microscopic simulation. The results show that the total delay in the network decreases significantly and the mean speed increases accordingly.

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**Keywords:** traffic signal control; saturated traffic condition; gating; network fundamental diagram; feedback control

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## 1. Introduction

Traffic congestion in urban road networks is a persisting or even increasing problem of modern society. Congestion can be reduced either by increasing road capacity (supply), or by reducing traffic demand. On the supply side, the provision of new infrastructure is not always a feasible solution, hence it is necessary to focus on a better utilization of the existing infrastructure (e.g. traffic management), to

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mitigate congestion and improve urban mobility. The field of urban traffic control (UTC) has been studied and developed in a variety of ways during the past decades. In fact, the traffic flow conditions in large-scale urban networks depend critically on the applied signal control strategies. However, as the debate regarding urban mobility and the wish for a sustainable transport system indicate, the negative effects of congested transport networks, such as excessive delays, environmental impact and reduced safety, persist or even increase; hence, introducing improved traffic signal control methods and techniques continues to be a vital issue. In particular, the development of practicable and efficient real-time signal control strategies for urban road networks under saturated traffic conditions is a major challenge with significant scientific and practical relevance. The scientific relevance stems from the recently increased interest in the specific problem as well as recent, potentially valuable, models and insights that may contribute to improved signal control methods. The practical relevance stems from the congestion, degradation and gridlock problems encountered increasingly in modern urban road networks that could benefit highly from improved signal control under saturated traffic conditions.

UTC systems constitute a scientific field with long-lasting and extensive research and development activities. Many methodologies have been proposed so far, but there is still space for new developments, particularly for saturated traffic conditions. In fact, widely used strategies like SCOOT (Hunt et al., 1982) and SCATS (Lowrie, 1982), although applicable to large-scale networks, are deemed less efficient under saturated traffic conditions. On the other hand, more advanced traffic-responsive strategies like OPAC (Gartner, 1983), PROLYN (Farges et al., 1983), and RHODES (Mirchandani and Head, 1998) use optimisation algorithms with exponential complexity, which do not permit a straightforward central network-wide application. Thus, most available strategies face limitations when it comes to saturated traffic conditions that are frequently observed in modern metropolitan areas. A noteworthy and practicable attempt to address saturated traffic conditions was the more recently developed signal control strategy TUC (Diakaki et al., 2002), see also (Aboudolas et al., 2010). Furthermore, a number of research approaches have been proposed, that employ various computationally expensive numerical solution algorithms, including genetic algorithms (Abu-Lebdeh and Benekohal, 1997; Lo et al., 2001), multi-extended linear complementary programming (De Schutter and De Moor, 1998), mixed-integer linear programming (Lo, 1999; Beard and Ziliaskopoulos, 2006) and ant colony optimisation (Putha et al., 2010); however, in view of the high computational requirements, the network-wide implementation of these optimization-based approaches might face some difficulties in terms of real-time feasibility. In fact, a recent FHWA report (as cited in (Lieberman et al., 2010)) opined: *“No current generally available tool is adequate for optimizing [signal] timing in congested conditions”*.

The notion of a fundamental diagram (e.g. in the form of a flow-density curve) for highways was recently found to apply (under certain conditions) to two-dimensional urban road networks as well; see (Gartner and Wagner, 2004) for simulation-based experiments; (Geroliminis and Daganzo, 2008) for real-data based investigations; (Daganzo and Geroliminis, 2008), (Farhi, 2008) and (Helbing, 2009) for analytical treatments. In fact, a fundamental-diagram-like shape of measurement points was first presented by (Godfrey, 1969), but also observed in a field evaluation study by (Dinopoulou et al., 2005), see Fig. 6 and the related comments therein. The concept is sometimes called MFD (macroscopic fundamental diagram), but since the ordinary fundamental diagram (for highways) is also macroscopic, we prefer to call it NFD (network fundamental diagram) for better distinction. Although the exact NFD curve may depend on the origin-destination demand (Ji et al., 2010), it may be quite stable from day to day, particularly if traffic load is homogeneously distributed in network links (Geroliminis and Sun, 2011). In simulated environments, where different signal control strategies are tested, this homogeneity condition may call for activation of a dynamic traffic assignment device to reduce possible transient phenomena, such as hysteresis during network filling and emptying (Aboudolas et al., 2010), (Geroliminis and Sun, 2011).

A practical tool, frequently employed against over-saturation of significant or sensitive links or urban network parts, is gating (Wood et al., 2002; Bretherton et al., 2003; Luk and Green, 2010). The idea is to hold traffic back (via prolonged red phases at traffic signals) upstream of the links to be protected from over-saturation, whereby the level or duration of gating may depend on real-time measurements from the protected links. The method is usually employed in an ad hoc way (based on engineering judgment and manual fine-tuning) regarding the specific gating policy and quantitative details, which may readily lead to insufficient or unnecessarily strong gating actions.

In this paper, the urban network NFD concept is exploited to improve mobility in saturated traffic conditions via application of gating measures, based on an appropriate feedback control structure. More specifically, the NFD is used to derive clear gating targets that maximize throughput in the protected network part; moreover, an appropriate simple dynamic model is developed, that allows for the straightforward derivation of simple but efficient feedback regulators, suitable for smooth and efficient operations. The proposed methodology is applied and demonstrated for the urban road network of Chania, Greece, in a microscopic simulation environment under realistic traffic conditions.

## 2. Methodology

### 2.1. General gating task

The objective of the presented methodology is to mitigate urban traffic congestion via feedback gating, by exploiting the notion of the network fundamental diagram (NFD) for an urban network part that needs to be protected from the detrimental effects of over-saturation. To gate the traffic flow (usually during the peak periods) in an urban network, the area to be protected from possible congestion and the locations where gating queues will be created, must be defined. The general scheme of gating, including the protected network (PN), is sketched in Fig. 1. To implement gating, the usual traffic lights settings must be modified at (one or more) upstream junctions, which may be located more or less close to the problematic area. In Fig. 1, the double line indicates the gating location, upstream of which vehicle queues may grow temporarily faster than without gating;  $q_g$  is the gated flow, a part of which ( $q_b$ ) may not be bound for the protected network (PN); while  $q_{in}$  is the part of the gated flow that enters the protected network;  $q_d$  represents other (non-gated or internal) inflows to the PN (disturbances); finally  $q_{out}$  and  $N$  stand for the PN exit flow (both internal and external) and the number of vehicles included in the PN, respectively.

If  $N$  is allowed to grow beyond certain limits, the PN exit flow  $q_{out}$  decreases (according to the NFD) due to link queue spillovers and gridlock. To avoid this PN degradation, gating should reduce the PN inflow  $q_{in}$  appropriately, so as to maximize the PN throughput. This may incur some temporary vehicle delays in the queues of the gated junctions, which, however, may be eventually offset (at least for the  $q_{in}$  portion of the gated flow) thanks to the higher PN exit flow enabled by gating; on the other hand, the flow  $q_b$  will experience gating delays without any direct reward; these delays will be generally smaller if the

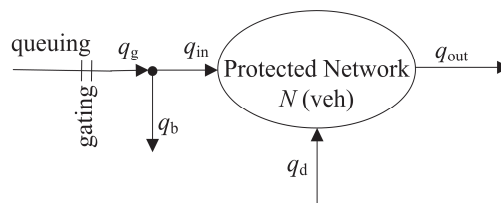


Fig. 1. General scheme of the protected network and gating.

gating junction is closer (or attached) to PN, due to accordingly smaller (or zero) flows  $q_b$ . In some situations, e.g. when major problems in PN may cause congestion to spread rapidly to adjoining areas, the use of gating could provide even higher benefits to the overall network.

## 2.2. Application network

In this study, the central business district (CBD) of the Chania urban road network, where the congestion usually starts during the peak period, is considered as the protected network. Eight gating links are specified exactly at the border of the protected network. A greater part of the Chania urban road network is modelled in the AIMSUN microscopic simulation environment (TSS, 2009), according to Fig. 2. The PN is separated from the rest of the network by the red border in Fig. 2. The PN consists of 165 links, while the 8 traffic junctions selected for gating are indicated by arrows in Fig. 2. In the middle of every link inside the red border line, a loop detector has been installed, and the related measurements are collected at every cycle (in this case 90 s). The gating links have been chosen to provide sufficient space for vehicle queuing, so that further upstream junctions are not significantly obstructed. As indicated with small circled links in Fig. 2, multiple origins and destinations are introduced at the network boundaries, but also at internal network locations, including the PN area. These origins and destinations (O-D) account for various corresponding in- and outflows, including on-street and off-street parking arrivals and departures, that may partially affect the PN area. The introduced O-D flows are realistic (based on real measurements) but not exact (particularly with regard to the used O-D rates).

When running AIMSUN, the tool's embedded real-time dynamic traffic assignment option is activated, as this is deemed to lead to a more realistic distribution of the demand within the network. In particular, if gating measures create long queues and delays at the gated links, alternative routes (if available) may be selected by the drivers; clearly, this reflects the medium-term routing behaviour of drivers to any introduced gating measures. Note also that this diversion may jeopardize to some extent the intended gating impact; therefore, the choice of gating links should also consider the availability and potential attractiveness of alternative routes that bypass the gating location.

## 2.3. Fundamental diagram of the PN

A network fundamental diagram may be an *ideal* NFD, if based on *exact* knowledge of the displayed quantities (this is practically only possible in analytic or simulation-based studies) for *all* links  $z \in Z$ ,

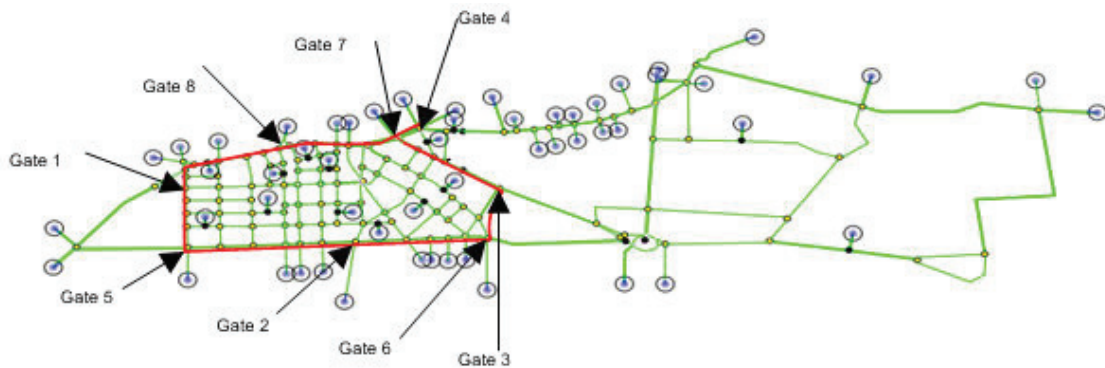


Fig. 2. Chania urban network modeled in AIMSUN.

where  $Z$  is the set of all network links; or an *operational* NFD, if based on available (more or less accurate) measurements and estimates at a subset  $M$  of all links, i.e.  $M \subseteq Z$ ; an operational NFD is called *complete*, if the measurements cover all network links, i.e. if  $M = Z$ .

The complete operational NFD of the Chania PN is obtained via a 4-hour AIMSUN simulation scenario with realistic O-D demands and dynamic traffic assignment based routing, and is displayed in Fig. 3. The NFD's y-axis reflects the Total Travelled Distance ( $TTD$  in veh·km per h), while the x-axis reflects the Total Time Spent ( $TTS$  in veh·h per h) by all vehicles in the PN. The  $TTD$  and  $TTS$  are obtained from the emulated loop measurements via the following equations:

$$TTS(k) = \sum_{z \in M} \frac{T \cdot \hat{N}_z(k)}{T} = \sum_{z \in M} \hat{N}_z(k) = \hat{N}(k) \quad (1)$$

$$TTD(k) = \sum_{z \in M} \frac{T \cdot q_z(k) \cdot L_z}{T} = \sum_{z \in M} q_z(k) \cdot L_z \quad (2)$$

where  $z$  is the link where a measurement is collected;  $M$  is the set of measurement links;  $k = 0, 1, 2, \dots$  is a discrete time index reflecting corresponding cycles;  $T$  is the cycle time;  $q_z$  is the measured flow in the link  $z$  during cycle  $k$ ;  $L_z$  is the length of link  $z$ ; and  $\hat{N}_z(k)$  is the estimated number of vehicles in link  $z$  during cycle  $k$ , which is derived from measured occupancy measurements via the following equation

$$\hat{N}_z(k) = L_z \cdot \frac{\mu_z}{100\lambda} \cdot o_z(k) \quad (3)$$

where  $o_z$  is the measured occupancy (in %) in link  $z$  during cycle  $k$ ;  $\mu_z$  is the number of lanes of link  $z$ ; and  $\lambda$  is the average vehicle length (in m). According to the derivations in (1) and (2),  $TTS$  equals the number of vehicles in all PN links equipped with detectors; while  $TTD$  is a length-weighted sum of the corresponding PN link flows.

Fig. 3(a) displays the (operational) NFD for the PN (assuming that all links are detector-equipped, i.e.  $M = Z$ ) for the first 2 hours of the employed scenario, i.e. the period during which the network is filled, and the congestion is created; 10 different replications (each with different seed in AIMSUN) were carried out. To build a comprehensive NFD that includes free-flow conditions, the specified demand starts from very low values and increases gradually to levels that lead to heavy congestion in PN (as under typical real traffic conditions at the peak periods); eventually, the demand is gradually reduced until the network is virtually emptied at the end of the simulation (see Fig. 3(b)). Fig. 3(a) demonstrates that a fundamental diagram (inverse-U) shape is indeed occurring during the 2-h network filling period, with quite moderate scatter even across different replications; Fig. 3(b) indicates that the inverse-U shape appears also during the decreasing demand period of 2 h, albeit with a visible hysteresis compared to the filling 2-h period. The hysteresis is limited and is due to different link load patterns that are present in the emptying period compared to the filling period. Whatever the exact NFD (and despite some limited scatter), it can be seen in Fig. 3 that the maximum  $TTD$  values in the diagram occur in a  $TTS$  region of 600 to 800 veh·h per h. If  $TTS$  (i.e.  $N$ ) is allowed to increase beyond this limit, then  $TTD$  (and hence the PN throughput) decreases; this leads to an unstable escalation, as long as the PN inflows continue to be higher, that degrades increasingly the PN capacity and efficiency, leading them to accordingly low levels (or even to zero in the extreme total-gridlock case). To avoid this unstable degradation and, in fact, maximize the PN throughput and efficiency, the PN's  $TTS$  should be maintained in the mentioned optimal range, and this is exactly the goal of this work.

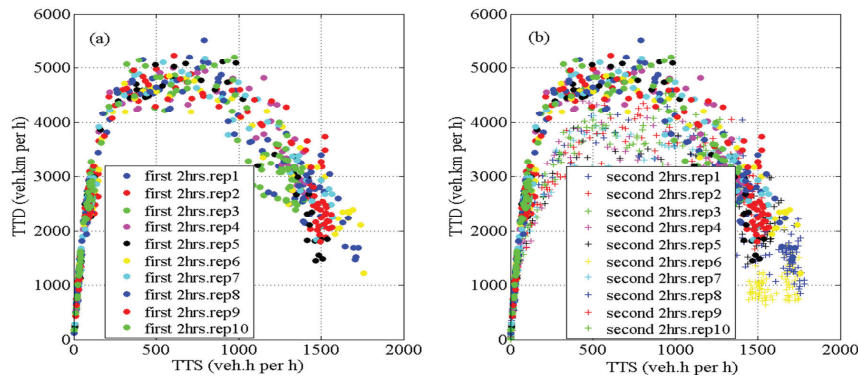


Fig. 3. (a) NFD of the PN for the first 2 hours for 10 replications; (b) NFD of PN for the 4 hours simulation for 10 replications.

#### 2.4. System modeling for feedback control design

Gating may be enabled via very simple, but highly efficient and robust feedback regulators that are well-known in Control Engineering. The regulators are strictly based on real-time measurements, without any need for online model or demand predictions. On the other hand, for a proper choice of the feedback structure (among several offered in classical feedback theory), it is essential to know the basic dynamics of the process under control, and this task is indeed rendered quite simple and easy when using the notion of the NFD.

The developed model and feedback controller structures are summarized in Fig. 4. The model input is the gated flow  $q_g$  (see Fig. 1); the model output is the PN's  $TTS$ ; while the main external disturbance is the uncontrolled PN inflow  $q_d$ . The model is first developed in a continuous-time environment for convenience. To start with, we have in the general case

$$q_{in}(t) = \beta \cdot q_g \cdot (t - \tau) \quad (4)$$

where  $\beta$  is the portion of gated flow ( $q_g$ ) that enters the PN;  $t$  is the time argument;  $\tau$  is the travel time needed for gated vehicles to approach the PN (when the gating link is not directly at the PN boundary). The conservation equation for vehicles in the PN (see Fig. 1) reads:

$$\dot{N}(t) = q_{in}(t) + q_d(t) - q_{out}(t). \quad (5)$$

As in the discrete-time case, we have also for the ideal values  $TTS_{id}(t) = N(t)$  (where  $N$  is the real number of vehicles within PN), but  $TTS$  in Fig. 4 denotes the operational value, which differs from the ideal value in two respects: firstly, detectors may not be available in each and every PN link, hence the operational  $TTS$  will be smaller by some factor  $A \leq 1$ ; secondly, the occupancy measurement and, most importantly, the estimation (3) may not be exact, hence we introduce a measurement/estimation error  $\varepsilon_1$ ; which finally yields

$$TTS(t) = A \cdot N(t) + \varepsilon_1(t). \quad (6)$$

From this operational  $TTS(t)$ , we may derive, using the operational NFD, the corresponding (operational)  $TTD$ , i.e.



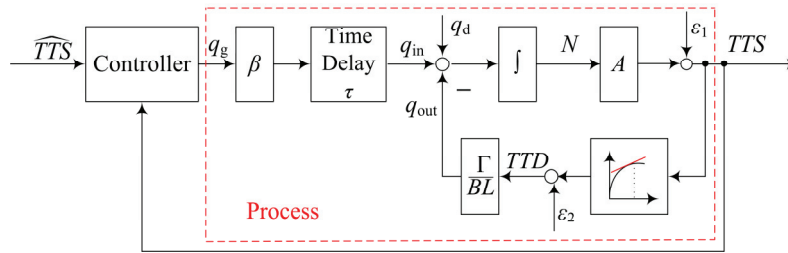


Fig. 4. Block diagram of the system and the feedback controller.

$$TTD(t) = F[TTS(t)] + \varepsilon_2 \quad (7)$$

where  $F(\cdot)$  is a nonlinear best-fit function of the operational NFD's measurement points, and  $\varepsilon_2$  denotes the corresponding fitting error (due to NFD scatter). Since  $TTD$  in (7) and Fig. 4 is the operational quantity, the ideal  $TTD_{id}$  (considering all PN links, not just the ones equipped with detectors) will be bigger, i.e.

$$TTD_{id}(t) \cdot B = TTD(t) \quad (8)$$

where  $B \leq 1$  is the flow-analogous factor of  $A$  earlier.

To proceed, we will now introduce the modelling assumption that the PN outflow  $q_{out}$  is proportional to  $TTD_{id}$ , i.e.

$$q_{out}(t) = \frac{\Gamma}{L} TTD_{id}(t) \quad (9)$$

where  $\Gamma$  is a sort of network exit rate,  $0 \leq \Gamma \leq 1$ , and  $L$  is the average PN link length. Replacing (8) in (9), we complete the process model derivation according to Fig. 4. The overall model (from  $q_g$  to  $TTS$ ) turns out to be a time-delayed nonlinear first-order system.

This model may be linearized around an optimal steady state that is within the aforementioned maximum  $TTD$  region of the NFD. Denoting steady-state variables with bars, we have

$$\bar{q}_{in} + \bar{q}_d = \bar{q}_{out} \quad (10)$$

$$\bar{q}_{out} = \frac{\Gamma}{BL} TTD \quad (11)$$

while  $\bar{\varepsilon}_1$  and  $\bar{\varepsilon}_2$  are set equal to zero. With the notation  $\Delta x = x - \bar{x}$  used analogously for all variables, the linearization yields

$$\frac{d}{dt}(\Delta TTS) = \left( \Delta q_{in} + \Delta q_d - \frac{\Gamma \bar{F}'}{BL} \Delta TTS \right) \cdot A + \varepsilon \quad (12)$$

where  $\varepsilon$  may be derived from the previous errors  $\varepsilon_1$  and  $\varepsilon_2$ , and  $\bar{F}'$  is the slope of the NFD at the optimal set-point  $TTS$ , i.e.  $TTS = \hat{TTS}$ . This set-point should be selected within the optimal  $TTS$ -range of the NFD, e.g. within [600, 800] for the Chania PN, for maximum efficiency. Note that  $\bar{F}'$  may be virtually equal to zero if the set-point is optimal; nevertheless, we will assume  $\bar{F}' > 0$  here, in order to enable

proper linearised modeling. This assumption has absolutely no impact on the employed regulator (14), whose operation is only governed by the regulation error  $\hat{TTS} - TTS$ .

The continuous-time state equation (12) of the protected network (using the conservation equation and the NFD) may be directly translated in discrete time as follows (Nise, 1995)

$$\Delta TTS(k+1) = \mu \cdot \Delta TTS(k) + \zeta \cdot [\Delta q_{in}(k) + \Delta q_d(k)] + \varepsilon(k) \quad (13)$$

where  $\mu = \exp(-\Gamma \bar{F}' TA / BL)$  and  $\zeta = (1 - \mu) BL / \Gamma \bar{F}'$ . It is trivial to include in these models the time delay, by replacing  $q_{in}$  from (4).

The derived simple model includes a number of parameters that have clear physical meaning; nevertheless, the precise value of some of these parameters may be difficult to obtain in practice, particularly if the PN is a sizeable network (as in the Chania example). However, the main reason for developing the gating model is to deduce the structure of the underlying dynamics, which is essential for the proper choice of the regulator structure.

### 2.5. Controller design

To avoid congestion-caused degradation (i.e. a *TTD* decrease), the critical value (i.e. the value of *TTS* at which the maximum *TTD* is attained) in the NFD is considered as the set value for the controller. The control goal is to keep the traffic state of the PN around the set value, so that *TTD* is maximized and the network does not enter the over-saturation area in the NFD according to Fig. 3. To this end, given the derived model structure in the previous section, the following proportional-integral-type (PI) feedback controller is well suitable

$$q_{in}(k) = q_{in}(k-1) - K_p [TTS(k-1) - TTS(k-2)] + K_I [\hat{TTS} - TTS(k-1)] \quad (14)$$

where  $K_p$  and  $K_I$  are the proportional and integral gains, respectively. Good regulator gain values may be found with appropriate Control Engineering methods or manual fine-tuning; model parameter estimation (e.g. of  $\mu$  and  $\zeta$  in (13)), by use of real  $q_{in}$  versus *TTS* measurements, may be useful in this endeavor; in any case, feedback regulators are quite robust to moderate parameter value changes.

If gating is applied at multiple links, the flow calculated by the (unique) regulator (14) must be split among the gated links according to some pre-specified policy (e.g. according to the respective saturation flows, as in the Chania application here). The flow calculated by the regulator (14) must be constrained by pre-specified minimum and maximum values to account for physical or operational constraints. For the lower bound, one may choose the flow corresponding to the minimum-green settings of the gated links (as in the Chania application here), or higher, e.g. if some gated links need to be protected from over-spilling. The upper bound has two components, a constant and a variable one, similarly to ALINEA ramp metering (Wang et al., 2010), and it is decided in real time which of the two is to be applied at each control step; the constant upper bound may be specified according to the maximum-green settings of the gated links (as in the Chania application here), or lower, e.g. if some downstream links need to be protected from over-spilling; the variable upper bound aims at activating the regulator more promptly under certain circumstances, see (Wang et al., 2010) for further details on the reasoning and method. It should be noted that, in the Chania application of this paper, upper and lower flow bounds are actually specified also for every individual gated link. If the regulator flow distribution is found to violate some of these individual bounds, then the surplus flows are re-distributed among the rest of the gated links.

Gating could be activated only within specific time windows (e.g. at the peak periods) or if some real-time measurement-based conditions are satisfied. After distributing the regulator-ordered flow to the gated links, the individual sub-flows must be converted to appropriate green times by modifying the usual



Table 1. Non-gating performance indexes for each replication.

	Rep.1	Rep.2	Rep.3	Rep.4	Rep.5	Rep.6	Rep.7	Rep.8	Rep.9	Rep.10	Ave.	Max	Min
Delay (s)	513	722	362	360	431	674	467	372	350	424	467	722	350
Speed (km/h)	6.62	5.05	8.91	8.88	7.81	5.55	7.25	8.84	9.06	7.83	7.58	9.06	5.05
Vehicles out	14545	12997	14575	14593	14771	11092	14684	14719	14338	14844	14115	14844	11092

traffic signal settings in the corresponding junctions. Note that the implemented flow may differ from the flow ordered by the regulator for a number of reasons, including limited accuracy of signal specification, low demand, over-spilling downstream link or flow constraints; however, the regulator is largely robust to these occurrences thanks to its feedback structure, as it will be demonstrated in the next section.

### 3. Results

The microscopic simulator AIMSUN is stochastic, thus different simulation runs (replications) with different random seeds may lead to different results. For this reason, it is common to use a number (10 in this work) of replications for each investigated scenario and then calculate the average value of the 10 runs for each evaluation criterion in order to compare different control cases with non-gated cases. Three performance indexes are used here (as provided by AIMSUN): the average vehicle delay per km; the mean speed in the entire Chania urban network (not only the PN); and the number of vehicles that exit the overall network during the whole scenario.

#### 3.1. Non-gating case

Signal control for the non-gating case corresponds to the usual fixed-time settings used in the real Chania network. Table 1 displays the aforementioned indexes for every replication; as well as for the average, maximum and minimum values of each index. Since AIMSUN is a stochastic tool, link over-spilling and partial gridlocks may be more or less pronounced in individual replications. In some replications (e.g. Rep. 2 and Rep. 6 in Table 1), the created congestion in the peak period leads to more serious gridlocks in the PN, consequently the delay is higher and the mean speed is lower than average, while the (lower) number of exited vehicles in these replications indicates that the network is not yet empty at the end of the simulation.

To enable an illustrative comparison of the non-gating versus gating cases, the respective detailed results of Replication 1 are displayed in Fig. 5, namely the PN's *TTS* (Figs. 5(a) and 5(d)), the PN inflow (from 8 gated links)  $q_{in}$  (Figs. 5(b) and 5(e)), and the PN's *TTD* (Figs. 5(c) and 5(f)). Concentrating on the left column of Fig. 5 (parts (a), (b), (c)), the 1<sup>st</sup> hour is characterized by a gradual increase of all three displayed quantities, as it is typical for increasing demand in under-saturated traffic conditions. At time  $t = 1$  h, the abrupt increase of  $q_{in}$  leads to according increases of *TTS* and *TTD*, the latter reaching soon capacity values according to Fig. 3(a), while the former is traversing the aforementioned critical region of [600, 800]. However, as  $q_{in}$  continues to be high, *TTS* continues to increase to very high values (i.e. the PN becomes increasingly crowded with vehicles); as a consequence, link over-spilling and gridlock lead to a sensible *TTD* reduction to low levels, that are persisting until  $t = 3$  h, when the network starts de-congesting due to low demand. Remarkably, during the congested period  $t \in [1.5 \text{ h}, 3 \text{ h}]$ , the inflow  $q_{in}$  is also reduced due to over-spilling links of PN, i.e. as a result of the congestion that extends beyond the PN.

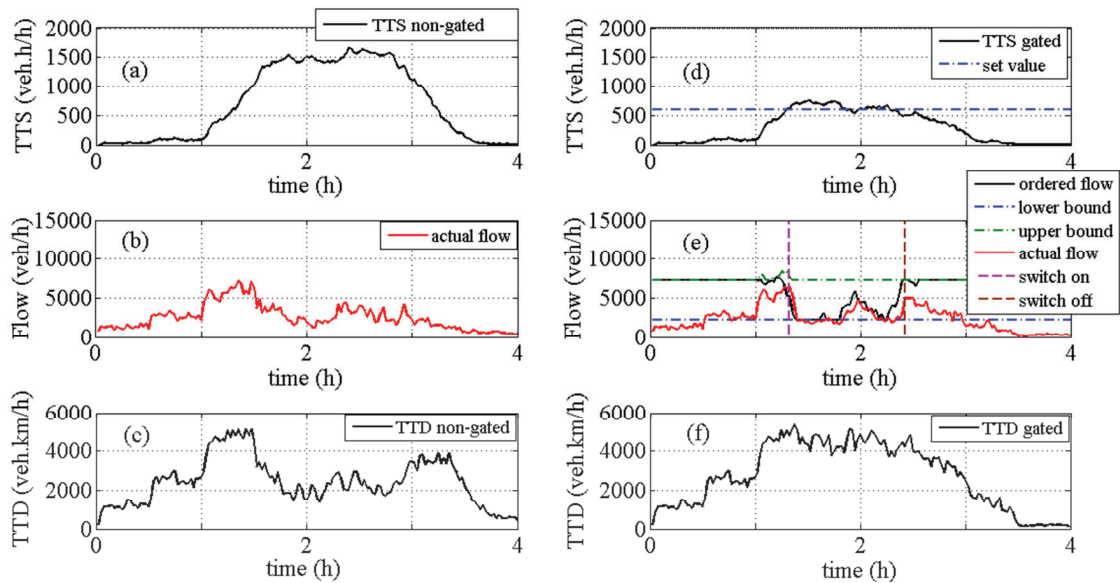


Fig. 5. (a) PN's *TTS* vs. time in non-gating case; (b) actual PN inflow vs. time for the non-gating case; (c) PN's *TTD* vs. time for the non-gating case; (d) PN's *TTS* vs. time for the gating case; (e) ordered and actual PN inflow vs. time for the gating case; (f) PN's *TTD* vs. time for the gated case.

### 3.2. Gating case

In the Chania gating example, the time delay  $\tau$  is zero, hence the  $K_p$  and  $K_i$  values may be specified for a dead-beat regulator behavior. To this end, a least-squares parameter estimation was conducted for  $\mu$  and  $\zeta$  in (13), using time-series of  $(q_{in}, TTS)$ -measurements within and around the critical *TTS*-range of [600, 800], which led to regulator gains  $K_p = 20 \text{ h}^{-1}$  and  $K_i = 5 \text{ h}^{-1}$ . The regulator's maximum and minimum bounds are visible in Fig. 5(e). The regulator runs continuously in the background, but gating is actually activated only when *TTS* exceeds a threshold, that is selected slightly lower than (in this case 85% of) the set point; and is de-activated when *TTS* falls below a 2<sup>nd</sup>, slightly lower threshold. At all other times, fixed-time signal control is applied, as in the non-gating case. A set point of  $TTS = 600 \text{ veh}\cdot\text{h}$  per h is selected for the gating operation.

By running AIMSUN with the control law (14) for the gated traffic signals, the results displayed in

Table 2. Performance indexes using the proposed gating control strategy.

	Rep.1	Rep.2	Rep.3	Rep.4	Rep.5	Rep.6	Rep.7	Rep.8	Rep.9	Rep.10	Ave.	Max	Min
Delay (s)	293	287	310	298	317	310	328	314	299	292	304	328	287
Upgrade (%)	42.8	60.2	14.4	17.2	26.5	54.0	29.8	15.6	14.6	31.1	35.0	54.0	14.4
Speed (km/h)	10.3	10.6	9.9	10.4	10.0	10.0	9.4	9.9	10.3	10.4	10.1	10.6	9.4
Upgrade (%)	55.6	110	11.1	17.1	28.0	80.2	29.7	12.0	13.7	32.8	39.2	110	11.1
Vehicles out	14721	14521	14623	14516	14508	14569	14783	14632	14441	14515	14582	14783	14441

Table 2 are obtained for each of the 10 replications. The improvements, compared to Table 1, are significant, and, in fact, even the worse gating replication is superior to the best non-gating replication. An average speed increase of 40% results for the whole network (not just the protected part thereof).

Figs. 5(d),(e),(f) display the detailed results of Replication 1 of the gating case and illustrate its way of functioning and impact. Traffic conditions are identical as in the non-gating case up to around  $t = 1.2$  h, when gating is switched on (Fig. 5(e)), as  $TTS$  approaches its set value; the gating regulator orders low inflow values to maintain  $TTS$  around its set point, and, as a consequence,  $TTD$  is maintained at high levels, in clear contrast to the non-gating case. It is visible in Fig. 5(e) that the  $q_{in}$  values ordered by the regulator, differ from the implemented ones for various reasons mentioned earlier, but this has a minor impact on the regulator's efficiency, as expected. At  $t = 2.3$  h,  $TTS$  is moving to lower values, gating is switched off, and traffic flow returns to under-saturated conditions; in contrast to the non-gating case where over-saturated conditions are seen in Fig. 5 to persist for 1 hour longer.

#### 4. Conclusion

A new traffic-responsive gating strategy, based on a simple but efficient PI feedback regulator, was developed for UTC under saturated conditions via exploitation of the NFD (network fundamental diagram) concept. The Chania urban network is modeled in the microscopic simulator AIMSUN as a test-bed for this research, to protect its most sensitive part from spillovers, gridlock, and the resulting strong degradation.

Application of the developed gating strategy is demonstrated to lead to significant improvements (in the order of 40%) compared to the non-gating control case. In this research, the measurements of all links within the PN are fed to the regulator; on-going research demonstrates that this is not necessary, and that gating may be applied similarly efficiently with far less real-time measurements. Further research directions include queue balancing and management at the gating positions, comparison with more comprehensive traffic-responsive signal control strategies, and, most importantly, field implementation of the proposed gating strategy.

#### Acknowledgments

The research leading to these results has been funded by the European Commission FP7 program, NEARCTIS (Network of Excellence for Advanced Road Cooperative traffic management in the Information Society).

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